NCERT Solutions for Class 7 Maths Chapter 9

Rational Numbers Class 7

Chapter 9 Rational Numbers Exercise 9.1, 9.2 Solutions

Exercise 9.1 : Solutions of Questions on Page Number : 182 Q1 : List five rational numbers between:

(i) - 1 and 0 (ii) - 2 and - 1

 $\frac{-4}{5} \text{ and } \frac{-2}{3} \text{ (iv) } \frac{1}{2} \text{ and } \frac{2}{3}$

Answer :

(i) - 1 and 0 $\frac{-1}{10}, \ \frac{-1}{20}, \ \frac{-1}{30}, \ \frac{-1}{40}, \ \frac{-1}{50}$

(ii) - 2 and - 1

$$-2 = \frac{-12}{6}$$
 and $-1 = \frac{-6}{6}$

Five rational numbers are

$$\frac{-11}{6}, \frac{-10}{6}, \frac{-9}{6}, \frac{-8}{6}, \frac{-7}{6}$$

$$\frac{-4}{5} \text{ and } \frac{-2}{3}$$

$$\frac{-4}{5} = \frac{-4 \times 9}{5 \times 9} = \frac{-36}{45} \text{ and } \frac{-2}{3} = \frac{-2 \times 15}{3 \times 15} = \frac{-30}{45}$$
Five rational numbers are

$$\frac{-35}{45}, \frac{-34}{45}, \frac{-33}{45}, \frac{-32}{45}, \frac{-31}{45}$$

$$\frac{1}{2} \text{ and } \frac{2}{3}$$

$$\frac{1}{2} = \frac{1 \times 18}{2 \times 18} = \frac{18}{36} \text{ and } \frac{2}{3} = \frac{2 \times 12}{3 \times 12} = \frac{24}{36}$$
Five rational numbers are

19	20	21	22	23
36'	36'	36'	36'	36

Q2 : Write four more rational numbers in each of the following patterns:

$$\frac{-3}{5}, \frac{-6}{10}, \frac{-9}{15}, \frac{-12}{20}, \dots \qquad \frac{-1}{4}, \frac{-2}{8}, \frac{-3}{12}, \dots$$

$$\frac{-1}{6}, \frac{2}{-12}, \frac{3}{-18}, \frac{4}{-24}, \dots \qquad \frac{-2}{3}, \frac{2}{-3}, \frac{4}{-6}, \frac{6}{-9}, \dots$$
(iii)

Answer :

$$\frac{-3}{5}, \frac{-6}{10}, \frac{-9}{15}, \frac{-12}{20}...$$
$$\frac{-3}{5}, \frac{-3 \times 2}{5 \times 2}, \frac{-3 \times 3}{5 \times 3}, \frac{-3 \times 4}{5 \times 4}....$$

It can be observed that the numerator is a multiple of 3 while the denominator is a multiple of 5 and as we increase them further, these multiples are increasing. Therefore, the next four rational numbers in this pattern are

$$\frac{-3\times5}{5\times5}, \frac{-3\times6}{5\times6}, \frac{-3\times7}{5\times7}, \frac{-3\times8}{5\times8}...$$
$$\frac{-15}{25}, \frac{-18}{30}, \frac{-21}{35}, \frac{-24}{40}...$$

(ii)

$$\frac{-1}{4}, \frac{-2}{8}, \frac{-3}{12}...$$
$$\frac{-1}{4}, \frac{-1 \times 2}{4 \times 2}, \frac{-1 \times 3}{4 \times 3}....$$

The next four rational numbers in this pattern are

$$\frac{-1\times4}{4\times4}, \frac{-1\times5}{4\times5}, \frac{-1\times6}{4\times6}, \frac{-1\times7}{4\times7} \dots$$

$$\frac{-4}{16}, \frac{-5}{20}, \frac{-6}{24}, \frac{-7}{28} \dots$$
(III)
$$\frac{-1}{6}, \frac{2}{-12}, \frac{3}{-18}, \frac{4}{-24} \dots$$

$$\frac{-1}{6}, \frac{1\times2}{-6\times2}, \frac{1\times3}{-6\times3}, \frac{1\times4}{-6\times4} \dots$$

The next four rational numbers in this pattern are

$$\frac{\frac{1\times5}{-6\times5}, \frac{1\times6}{-6\times6}, \frac{1\times7}{-6\times7}, \frac{1\times8}{-6\times8}...}{\frac{5}{-30}, \frac{6}{-36}, \frac{7}{-42}, \frac{8}{-48}...}$$

$$\frac{-2}{3}, \frac{2}{-3}, \frac{4}{-6}, \frac{6}{-9} \cdots$$
$$\frac{-2}{3}, \frac{2}{-3}, \frac{2 \times 2}{-3 \times 2}, \frac{2 \times 3}{-3 \times 3} \cdots$$

The next four rational numbers in this pattern are

$$\frac{2 \times 4}{-3 \times 4}, \frac{2 \times 5}{-3 \times 5}, \frac{2 \times 6}{-3 \times 6}, \frac{2 \times 7}{-3 \times 7} \dots$$
$$\frac{8}{-12}, \frac{10}{-15}, \frac{12}{-18}, \frac{14}{-21} \dots$$

Q3 :

Give four rational numbers equivalent to:

$$\frac{-2}{7}$$
 $\frac{5}{-3}$ $\frac{4}{9}$

Answer :

(i)
$$\frac{-2}{7}$$

Four rational numbers are

$$\frac{-2 \times 2}{7 \times 2}, \frac{-2 \times 3}{7 \times 3}, \frac{-2 \times 4}{7 \times 4}, \frac{-2 \times 5}{7 \times 5}$$
$$\frac{-4}{14}, \frac{-6}{21}, \frac{-8}{28}, \frac{-10}{35}$$
$$\frac{5}{-3}$$

Four rational numbers are

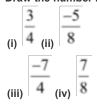
$\frac{3 \times 4}{25}$
25
2' -15

Four rational numbers are

4×2	2 4×	3 4	×4	4×5
9×2	2'9×	3'9	×4	9×5
8	12	16	20)
18	27'	36	45	5

Q4 :

Draw the number line and represent the following rational numbers on it:

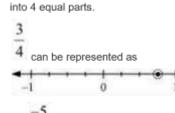


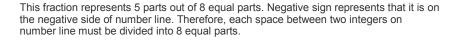


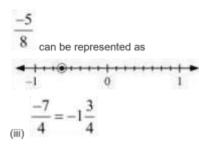
(ii) 8

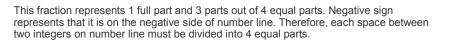


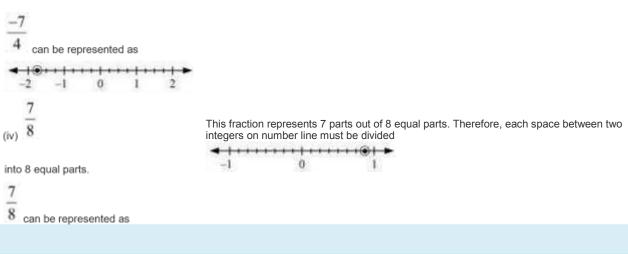
This fraction represents 3 parts out of 4 equal parts. Therefore, each space between two integers on number line must be divided







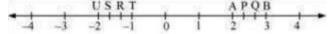




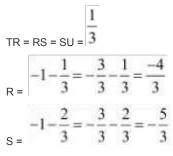
Q5 :

The points P, Q, R, S, T, U, A and B on the number line are such that,

TR = RS = SU and AP = PQ = QB. Name the rational numbers represented by P, Q, R and S.



Distance between U and T = 1 unit It is divided into 3 equal parts.



Similarly,

AB = 1 unit

It is divided into 3 equal parts.

$$P = 2 + \frac{1}{3} = \frac{6}{3} + \frac{1}{3} = \frac{7}{3}$$

$$Q = 2 + \frac{2}{3} = \frac{6}{3} + \frac{2}{3} = \frac{8}{3}$$

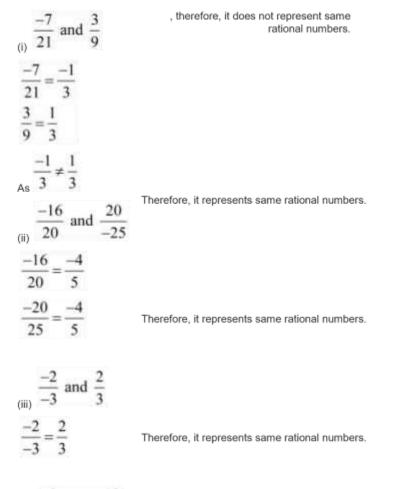
Q6 :

Which of the following pairs represent the same rational number?

$$\frac{-7}{21} \text{ and } \frac{3}{9} \underset{\text{(ii)}}{\stackrel{-16}{20}} \frac{-16}{-25} \underset{\text{(iii)}}{\stackrel{-2}{-3}} \frac{-2}{-3} \text{ and } \frac{2}{3}$$

$$\frac{-3}{5} \text{ and } \frac{-12}{20} \underset{\text{(v)}}{\stackrel{-5}{-5}} \frac{-3}{-5} \text{ and } \frac{-2}{15} \underset{\text{(vi)}}{\stackrel{-2}{-3}} \frac{1}{3} \text{ and } \frac{-1}{9}$$

$$\frac{-5}{-9} \text{ and } \frac{5}{-9}$$



$$\frac{-3}{5} \text{ and } \frac{-12}{20}$$

 $\frac{-12}{20} = \frac{-3}{5}$

Therefore, it represents same rational numbers.

$$\frac{\frac{8}{-5} \text{ and } \frac{-24}{15}}{\frac{-24}{15} = \frac{-8}{5}}$$

$$\frac{\frac{-24}{15} = \frac{-8}{5}}{\frac{8}{-5} = \frac{-8}{5}}$$
, therefore, it does not represent same rational numbers.

$$\frac{\frac{-5}{-9} \text{ and } \frac{5}{-9}}{\frac{-9}{-9}}$$
(vi) $\frac{1}{3}$ and $\frac{-1}{9}$

$$\frac{\frac{-5}{-9} = \frac{5}{9}}{\frac{-9}{9}}$$
As $\frac{5}{9} \neq \frac{-5}{9}$, therefore, it does not represent same rational numbers.

Q7 :

Rewrite the following rational numbers in the simplest form:

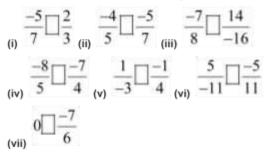
$$\frac{\frac{-8}{6}}{\frac{-44}{72}} \frac{\frac{25}{45}}{\frac{-8}{10}}$$

Answer :

$$\frac{-8}{6} = \frac{-4 \times 2}{3 \times 2} = \frac{-4}{3}$$
(i) $\frac{25}{45} = \frac{5 \times 5}{9 \times 5} = \frac{5}{9}$
(ii) $\frac{-44}{72} = \frac{-11 \times 4}{18 \times 4} = \frac{-11}{18}$
(iii) $\frac{-8}{10} = \frac{-4 \times 2}{5 \times 2} = \frac{-4}{5}$

Q8 :

Fill in the boxes with the correct symbol out of >, <, and =



$\frac{-5}{7} = \frac{-5 \times 3}{7 \times 3} = \frac{-15}{21}$
$\frac{2}{3} = \frac{2 \times 7}{3 \times 7} = \frac{14}{21}$
3 3×7 21
As - 15 < 14,
$\frac{-5}{7} \leq \frac{2}{3}$
Therefore, 7 3
(ii)
-4 -4×7 -28
$\frac{-4}{5} = \frac{-4 \times 7}{5 \times 7} = \frac{-28}{35}$
$\frac{-5}{7} = \frac{-5 \times 5}{7 \times 5} = \frac{-25}{35}$
$\overline{7} = \overline{7 \times 5} = \overline{35}$
As - 28 < - 25
-45
Therefore, $\frac{-4}{5} \le \frac{-5}{7}$
14 7 - 2 7 -7
(iii) Here, $\frac{14}{-16} = \frac{7 \times 2}{-8 \times 2} = \frac{7}{-8} = \frac{-7}{8}$
$\frac{-7}{8} \equiv \frac{14}{-16}$
Therefore, 816
(iv)
-8 -8×4 -32
$\frac{-8}{5} = \frac{-8 \times 4}{5 \times 4} = \frac{-32}{20}$
-7 -7×5 -35
$\frac{-7}{4} = \frac{-7 \times 5}{4 \times 5} = \frac{-35}{20}$
As - 32 > - 35,
-8 -7
Therefore, $5 \ge 4$
(v) −1 −1×4 −4
$\frac{-1}{3} = \frac{-1 \times 4}{3 \times 4} = \frac{-4}{12}$
$\frac{-1}{4} = \frac{-1 \times 3}{4 \times 3} = \frac{-3}{12}$
As - 4 < - 3,
$\frac{-1}{2} \leq \frac{-1}{4}$
$\frac{-1}{3} \leq \frac{-1}{4}$

(vi)
$$\frac{5}{-11} \equiv \frac{-5}{11}$$
(vi)
$$0 \geq \frac{-7}{6}$$

Q9 :

Which is greater in each of the following?

$$\begin{array}{c} \frac{2}{3}, \frac{5}{2}, \frac{-5}{6}, \frac{-4}{3}, \frac{-3}{4}, \frac{2}{-3}\\ \\ \frac{-1}{4}, \frac{1}{4}, \frac{-3}{7}, -3\frac{2}{7}, -3\frac{4}{5} \end{array}$$

Answer :

$$\frac{2}{3}, \frac{5}{2}$$

By converting these into like fractions,

$$\frac{2}{3} = \frac{2 \times 2}{3 \times 2} = \frac{4}{6}$$

$$\frac{5}{2} = \frac{5 \times 3}{2 \times 3} = \frac{15}{6}$$
As 15 > 4, therefore, $\frac{5}{2}$ is greater.

$$\frac{-5}{6}, \frac{-4}{3}$$

$$\frac{-4}{3} = \frac{-4 \times 2}{3 \times 2} = \frac{-8}{6}$$
As - 5 > -8, therefore, $\frac{-5}{6}$ is greater.
(iii)

$$\frac{-3}{4}, \frac{2}{-3}$$
Or, $\frac{-3}{4}, \frac{-2}{3}$

By converting these into like fractions,

$$\frac{-3}{4} = \frac{-3 \times 3}{4 \times 3} = \frac{-9}{12}$$

$$\frac{-2}{3} = \frac{-2 \times 4}{3 \times 4} = \frac{-8}{12}$$
As - 8 > -9, therefore, $\frac{-2}{3}$ is greater.
$$\left(\frac{-1}{4}, \frac{1}{4}, \frac{$$

By converting these into like fractions,

$$\frac{-23}{7} = \frac{-23 \times 5}{7 \times 5} = \frac{-115}{35}$$
$$\frac{-19}{5} = \frac{-19 \times 7}{5 \times 7} = \frac{-133}{35}$$
As - 115 > -133, therefore, -3 $\frac{2}{7}$ is greater.

Q10 : Write the following rational numbers in ascending order:

$$\frac{-3}{5}, \frac{-2}{5}, \frac{-1}{5}, \frac{-1}{3}, \frac{-1}{3}, \frac{-2}{9}, \frac{-4}{3}, \frac{-3}{7}, \frac{-3}{2}, \frac{-3}{4}$$

Answer :

$$\frac{-3}{5}, \frac{-2}{5}, \frac{-1}{5}$$
As - 3 < -2 < - 1,
$$\frac{-3}{5} < \frac{-2}{5} < \frac{-1}{5}$$

$$\frac{-1}{3}, \frac{-2}{9}, \frac{-4}{3}$$
(ii)

By converting these into like fractions,

$\frac{-1\times 3}{2}$.		
3×3 '		3×3
$\frac{-3}{9}, \frac{-2}{9}$	_	2
As - 12 < -	3 < - 2	2,
$\therefore \frac{-4}{2} <$	$\frac{-1}{-1}$	$\frac{-2}{2}$
3	3	9
(iii) $\frac{-3}{7}$,	$\frac{-3}{2}$,	$\frac{-3}{4}$

By converting these into like fractions,

-	3×4	-3×	14	-3×7
7	$\times 4$	2×	14	4×7
-	12 -	-42 -	-21	
2	8 '	28 '	28	
As -	42 <	- 21 <	- 12.	
	- 3	3		
		$\left(\frac{-3}{4}\right)$		
	4	4	1	

Exercise 9.2 : Solutions of Questions on Page Number : 190

Q1 :

Find the sum:

$$\frac{4}{5} + \left(\frac{-11}{4}\right)_{(ii)} \frac{5}{3} + \frac{3}{5}_{(iii)} \frac{-9}{10} + \frac{22}{15}$$

$$\frac{-3}{-11} + \frac{5}{9}_{(v)} \frac{-8}{19} + \frac{(-2)}{57}_{(vi)} \frac{-2}{3} + 0$$

$$\frac{-2}{3} + 4\frac{3}{5}$$
(vii)

Answer :

 $(i)45+(-11\ 4)=45-11\ 4=16-5520=-39\ 20$

$$\frac{5}{3} + \frac{3}{5}$$

L.C.M of 3 and 5 is 15.

5	3	5×5	3×3	25	9	25 + 9	34
3	5	3×5	5×3	15	15	15	15

(iii)
$$\frac{-9}{10} + \frac{22}{15}$$

L.C.M of 10 and 15 is 30.

L.O.WI OF TO and	10 18 50.					
$\frac{-9}{10} + \frac{22}{15} = \frac{-9}{10}$	-9×3 22	2×2	-27	44	-27 + 44	17
10 15 1	0×3 15	×2	30	30	30	30
$\frac{-3}{-11} + \frac{5}{9}$	$=\frac{3}{11}+\frac{5}{9}$					
L.C.M of 11 and	9 is 99.					
$\frac{3}{11} + \frac{5}{9} = \frac{3}{11}$	$\frac{\langle 9}{\times 9} + \frac{5 \times 1}{9 \times 1}$	$\frac{1}{1} = \frac{27}{99}$	$+\frac{55}{99}$	$=\frac{27+}{99}$	$\frac{55}{9} = \frac{82}{99}$	
$(v) \frac{-8}{19} + \frac{(-2)}{57}$	$\frac{)}{}=-\frac{8}{19}-$	$\frac{2}{57}$				
L.C.M of 19 and	57 is 57.					
8 2	8×3	2	24	2	-24-2	-26
$-\frac{8}{19}-\frac{2}{57}=$	19×3	57	57	57	57	57
$\frac{-2}{3} + 0 =$	$\frac{-2}{3}$					
(vii) $-2\frac{1}{3}+4$	$\frac{3}{5} = \frac{-7}{3} +$	$\frac{23}{5}$				
L.C.M of 3 and 5	is 15.					
$\frac{-7}{3} + \frac{23}{5} = \frac{-7}{5}$	-7×5 23	3×3_	-35	69	-35 + 69	34
3 5	3×5 5	×3	15	15	15	15

Q2 : Find

Find $\frac{7}{24} - \frac{17}{36} = \frac{5}{63} - \left(\frac{-6}{21}\right) = \frac{-6}{13} - \left(\frac{-7}{15}\right) = \frac{-3}{10} - \left(\frac{-7}{15}\right) = \frac{-3}{10} - \frac{7}{11} = \frac{-2}{9} - 6$ (iv) Answer

Answer :
7 17
(i) 24 36
L.C.M of 24 and 36 is 72.
7 17 7×3 17×2 21 34 21-34 -13
$\frac{7}{24} - \frac{17}{36} = \frac{7 \times 3}{24 \times 3} - \frac{17 \times 2}{36 \times 2} = \frac{21}{72} - \frac{34}{72} = \frac{21 - 34}{72} = \frac{-13}{72}$
(ii) $\frac{5}{63} - \left(\frac{-6}{21}\right) = \frac{5}{63} + \frac{2}{7}$
L.C.M of 63 and 7 is 63.
$\frac{5}{63} + \frac{2}{7} = \frac{5}{63} + \frac{2 \times 9}{7 \times 9} = \frac{5}{63} + \frac{18}{63} = \frac{5 + 18}{63} = \frac{23}{63}$
(iii) $\frac{-6}{13} - \left(\frac{-7}{15}\right) = \frac{-6}{13} + \frac{7}{15}$
L.C.M of 13 and 15 is 195.
$\frac{-6}{13} + \frac{7}{15} = \frac{-6 \times 15}{13 \times 15} + \frac{7 \times 13}{15 \times 13} = \frac{-90}{195} + \frac{91}{195} = \frac{-90 + 91}{195} = \frac{1}{195}$
-3 7
$\frac{-3}{8} - \frac{7}{11}$
L.C.M of 8 and 11 is 88.
-3 7 3×11 7×8 33 56 -33-56 -89
$\frac{-3}{8} - \frac{7}{11} = -\frac{3 \times 11}{8 \times 11} - \frac{7 \times 8}{11 \times 8} = -\frac{33}{88} - \frac{56}{88} = \frac{-33 - 56}{88} = \frac{-89}{88}$
1 19 6
$\begin{array}{c} -2\frac{1}{9} - 6 = -\frac{19}{9} - \frac{6}{1} \\ \end{array}$
L.C.M of 9 and 1 is 9.
19 6 19 6×9 19 54 -19-54 -73
$-\frac{19}{9} - \frac{6}{1} = -\frac{19}{9} - \frac{6 \times 9}{1 \times 9} = -\frac{19}{9} - \frac{54}{9} = \frac{-19 - 54}{9} = \frac{-73}{9}$

Q3 :

Find the product:

$$\frac{9}{2} \times \left(\frac{-7}{4}\right)_{(ii)} \frac{3}{10} \times (-9)_{(iii)} \frac{-6}{5} \times \frac{9}{11} \\ \frac{3}{7} \times \left(\frac{-2}{5}\right)_{(v)} \frac{3}{11} \times \frac{2}{5}_{(vi)} \frac{3}{-5} \times \frac{-5}{3}$$

Answer :

$$\begin{array}{c} \frac{9}{2} \times \left(\frac{-7}{4}\right) = \frac{9 \times (-7)}{2 \times 4} = \frac{-63}{8} \\ (i) & \frac{3}{10} \times \left(-9\right) = \frac{3}{10} \times \frac{(-9)}{1} = \frac{3 \times (-9)}{10 \times 1} = \frac{-27}{10} \\ \frac{3}{10} \times \left(-9\right) = \frac{3}{10} \times \frac{(-9)}{1} = \frac{3 \times (-9)}{10 \times 1} = \frac{-27}{10} \\ (ii) & \frac{-6}{5} \times \frac{9}{11} = \frac{-6 \times 9}{5 \times 11} = \frac{-54}{55} \\ \frac{3}{11} \times \frac{2}{5} = \frac{3 \times 2}{11 \times 5} = \frac{6}{55} \\ (v) & \frac{3}{-5} \times \frac{-5}{3} = \frac{3 \times (-5)}{(-5) \times 3} = \frac{-15}{-15} = 1 \end{array}$$

Q4 :

Find the value of:

(i)
$$(-4) \div \frac{2}{3} = \frac{-3}{5} \div 2 = \frac{-4}{5} \div (-3)$$

(ii) $\frac{-1}{8} \div \frac{3}{4} = \frac{-2}{13} \div \frac{1}{7} = \frac{-7}{12} \div \left(\frac{-2}{13}\right)$
(iv) $\frac{3}{13} \div \left(\frac{-4}{65}\right)$

(i)

$$-4 \div \frac{2}{3} = -4 \times \frac{3}{2} = \frac{-12}{2} = -6$$
(ii)

$$\frac{-3}{5} \div 2 = \frac{-3}{5} \times \frac{1}{2} = \frac{-3 \times 1}{5 \times 2} = \frac{-3}{10}$$
(iii)

$$\frac{-4}{5} \div (-3) = \frac{-4}{5} \times \frac{1}{-3} = \frac{(-4) \times 1}{5 \times (-3)} = \frac{-4}{-15} = \frac{4}{15}$$
(iii)

$$\frac{-1}{8} \div \frac{3}{4} = \frac{-1}{8} \times \frac{4}{3} = \frac{-1 \times 4}{8 \times 3} = \frac{-4}{24} = -\frac{1}{6}$$
(iv)

$$\frac{-2}{13} \div \frac{1}{7} = \frac{-2}{13} \times 7 = \frac{-14}{13}$$
(v)

$$\frac{-7}{12} \div \left(\frac{-2}{13}\right) = \frac{-7}{12} \times \frac{13}{-2} = \frac{(-7) \times 13}{12 \times (-2)} = \frac{-91}{-24} = \frac{91}{24}$$
(vi)

$$\frac{3}{13} \div \left(\frac{-4}{65}\right) = \frac{3}{13} \times \frac{65}{-4} = \frac{3 \times 65}{13 \times (-4)} = \frac{195}{-52} = -\frac{15}{4}$$