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## Linear Equations in Two Variables

### Exercise 4.1

**Write the correct answer in each of the following:**

- 1. The linear equation  $2x - 5y = 7$  has**

(A) A unique solution  
(B) Two solutions  
(C) Infinitely many solutions  
(D) No solution

**Sol.**  $2x - 5y = 7$  is a linear equation in two variables. A linear equation in two variables has infinitely many solution.  
Hence, (c) is the correct answer.

- 2. The equation  $2x + 5y = 7$  has a unique solution, if  $x, y$  are:**

(A) Natural numbers  
(B) Positive real numbers  
(C) Real numbers  
(D) Rational numbers

**Sol.** The equation  $2x + 5y = 7$  has a unique solution if  $x, y$  are natural numbers.  
Hence, (a) is the correct answer.

- 3. If  $(2, 0)$  is a solution of the linear equation  $2x + 3y = k$ , then the value of  $k$  is**

(A) 4  
(B) 6  
(C) 5  
(D) 2

**Sol.** Substituting  $x = 2$  and  $y = 0$  in the given equation  $2x + 3y = k$ , we get  
 $2(2) + 3(0) = k \Rightarrow k = 4$   
Therefore, the value of  $k$  is 4.  
Hence, (a) is the correct answer.

- 4. Any solution of the linear equation  $2x + 0y + 9 = 0$  in two variables is of the form:**

(a)  $\left(-\frac{9}{2}, m\right)$   
(b)  $\left(n, -\frac{9}{2}\right)$   
(c)  $\left(0, -\frac{9}{2}\right)$   
(d)  $(-9, 0)$

**Sol.** The given linear equation is  $2x + 0y + 9 = 0 \Rightarrow 2x = -9$   
 $\therefore x = -\frac{9}{2}$

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Since the coefficient of  $y$  is 0 in the given equation, the solution can be given as  $\left(-\frac{9}{2}, m\right)$ .

Hence, (a) is the correct answer.

**5. The graph of the linear equation  $2x + 3y = 6$  cuts the  $y$ -axis at the point**

- (A) (2, 0)
- (B) (0, 3)
- (C) (3, 0)
- (D) (0, 2)

**Sol.** The graph of the linear equation  $2x + 3y = 6$  cuts the  $y$ -axis at the point where  $x$ -coordinate is zero.

Putting  $x = 0$  in  $2x + 3y = 6$ , we get

$$2(0) + 3y = 6 \Rightarrow 3y = 6 \Rightarrow y = 6 \div 3 = 2$$

So, (0, 2) is the required point.

Hence, (d) is the correct answer.

**6. The equation  $x = 7$ , in two variables, can be written as**

- (A)  $1.x + 1.y = 7$
- (B)  $1.x + 0.y = 7$
- (C)  $0.x + 1.y = 7$
- (D)  $0.x + 0.y = 7$

**Sol.** The equation  $x = 7$  in two variables can be expressed as  $1.x + 0.y = 7$ .

Hence, (b) is the correct answer.

**7. Any point on the  $x$ -axis is of the form**

- (A) (x, y)
- (B) (0, y)
- (C) (x, 0)
- (D) (x, x)

**Sol.** Any point on the  $x$ -axis has its ordinate 0.

So, any point on the  $x$ -axis is of the form (x, 0).

Hence, (c) is the correct answer.

**8. Any point on the line  $y = x$  is of the form**

- (A) (a, a)
- (B) (0, a)
- (C) (a, 0)
- (D) (a, -a)

**Sol.** Any point on the line  $y = x$  will have  $x$  and  $y$  coordinate same.

So, any point on the line  $y = x$  is of the form (a, a).

Hence, (a) is the correct answer.

**9. The equation of  $x$ -axis is of the form**

- (A)  $x = 0$
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- (B)  $y = 0$   
(C)  $x + y = 0$   
(D)  $x = y$

**Sol.**  $y = 0$  is the equation of x-axis.  
Hence, (b) is the correct answer.

**10. The graph of  $y = 6$  is a line**

- (A) parallel to x-axis at a distance 6 units from the origin  
(B) parallel to y-axis at a distance 6 units from the origin  
(C) making an intercept 6 on the x-axis.  
(D) making an intercept 6 on both the axes.

**Sol.** The given equation  $y = 6$  does not contain x. Its graph is a line parallel to x-axis.  
So, the graph of  $y = 6$  is a line parallel to x-axis at a distance 6 units from the origin.  
Hence, (a) is the correct answer.

**11.  $x = 5, y = 2$  is a solution of the linear equation**

- (A)  $x + 2y = 7$   
(B)  $5x + 2y = 7$   
(C)  $x + y = 7$   
(D)  $5x + y = 7$

**Sol.**  $x = 5, y = 2$  is a solution of the linear equation  $x + y = 7$ , as  $5 + 2 = 7$ .  
Hence, (c) is a correct answer.

**12. If a linear equation has solutions  $(-2, 2)$ ,  $(0, 0)$  and  $(2, -2)$ , then it is of the form**

- (A)  $y - x = 0$   
(B)  $x + y = 0$   
(C)  $-2x + y = 0$   
(D)  $-x + 2y = 0$

**Sol.** The points  $(-2, 2)$  and  $(2, -2)$  have x and y coordinates of opposite signs.  
Also, any point on the graph of  $x + y = 0$   
i.e.,  $y = -x$  will have x and y coordinate of opposite signs. The Point  $(0, 0)$  also satisfies  $x + y = 0$ .  
Hence, (b) is the correct answer.

**13. The positive solutions of the equation  $ax + by + c = 0$  always lie in the**

- (A) 1st quadrant  
(B) 2nd quadrant  
(C) 3rd quadrant  
(D) 4th quadrant

**Sol.** Quadrant I consist of all points  $(x, y)$  for which the x and y are positive.  
So, the positive solution of the equation  $ax + by + c = 0$  always lie in the 1st quadrant.  
Hence, (a) is the correct answer.

**14. The graph of the linear equation  $2x + 3y = 6$  is a line which meets the x-axis at the point**

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(A) (0, 2)

(B) (2, 0)

(C) (3, 0)

(D) (0, 3)

**Sol.** The graph of the linear equation  $2x + 3y = 6$  is a line which meets the x-axis at the point where  $y = 0$ .

Now putting  $y = 0$  in  $2x + 3y = 6$ , we get

$$2x + 3(0) = 6 \Rightarrow 2x = 6 \Rightarrow x = 6 \div 2 = 3$$

So, (3, 0) is a point on the line  $2x + 3y = 6$ .

Hence, (c) is the correct answer.

**15. The graph of the linear equation  $y = x$  passes through the point.**

(a)  $\left(\frac{3}{2}, \frac{-3}{2}\right)$

(b)  $\left(0, \frac{3}{2}\right)$

(c) (1, 1)

(d)  $\left(\frac{-1}{2}, \frac{1}{2}\right)$

**Sol.** We know that any point on the line  $y = x$  will have x and y coordinates same.

So, the graph of the linear equation  $y = x$  passes through the point (1, 1).

Hence, (c) is the correct answer.

**16. If we multiply or divide both sides of a linear equation with a non-zero number, then the solution of the linear equation:**

(A) Changes

(B) Remains the same

(C) Changes in case of multiplication only

(D) Changes in case of division only

**Sol.** If we multiply or divide both sides of a linear equation with a non-zero number, then the solution of the linear equation remains the same.

Hence, (b) is the correct answer.

**17. How many linear equations in x and y can be satisfied by  $x = 1$  and  $y = 2$ ?**

(A) Only one

(B) Two

(C) Infinitely many

(D) Three

**Sol.** There are infinitely many linear equations which are satisfied by  $x = 1$  and  $y = 2$ .

For example, a linear equation  $x + y = 3$  is satisfied by  $x = 1$  and  $y = 2$ .

Others are  $y = 2x$ ,  $y - x = 1$ ,  $2y - x = 3$  etc.

Hence, (c) is the correct answer.

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**18. The point of the form (a, a) always lies on:**

- (A) x-axis
- (B) y-axis
- (C) On the line  $y = x$
- (D) On the line  $x + y = 0$

**Sol.** The points of the form (a, a) have x and y coordinates same. So, the point of the form (a, a) always lies on the line  $y = x$ .  
Hence, (c) is the correct answer.

**19. The point of the form (a, -a) always lies on the line**

- (A)  $x = a$
- (B)  $y = -a$
- (C)  $y = x$
- (D)  $x + y = 0$

**Sol.** The point of the (a, -a) have x and y coordinate of opposite signs.  
So, the points of the form (a, -a) always lie on the line  $y = -x$ , i.e.,  $x + y = 0$ .  
Hence, (d) is the correct answer.

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## Linear Equations in Two Variables

### Exercise 4.2

Write whether the following statements are true or false. Justify your answer.

1. **The point (0, 3) lies on the graph of the linear equation  $3x + 4y = 12$ .**

**Sol.** Substituting  $x = 0$  and  $y = 3$  in the equation

$$3(0) + 4(3) = 12 \Rightarrow 12 = 12, \text{ which is true.}$$

The point (0, 3) satisfies the equation  $3x + 4y = 12$ .

Hence, the given statement is true.

2. **The graph of the linear equation  $x + 2y = 7$  passes through the point (0, 7).**

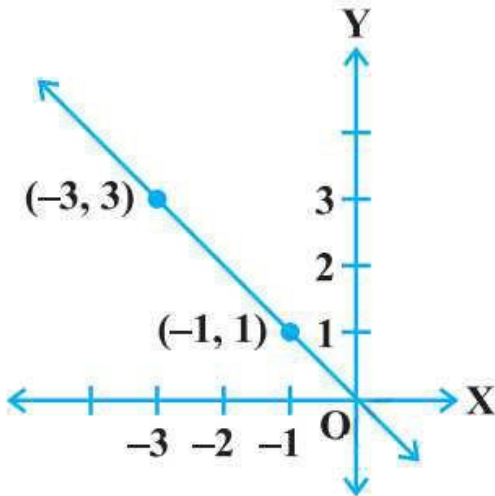
**Sol.** Substituting  $x = 0$  and  $y = 7$  in the given equation  $x + y + 2y = 7$ , we get

$$0 + 2(7) = 7 \Rightarrow 14 = 7, \text{ which is false.}$$

The point (0, 7) does not satisfy the equation.

Hence, the given statement is false.

3. **The graph given below represents the linear equation  $x + y = 0$ .**



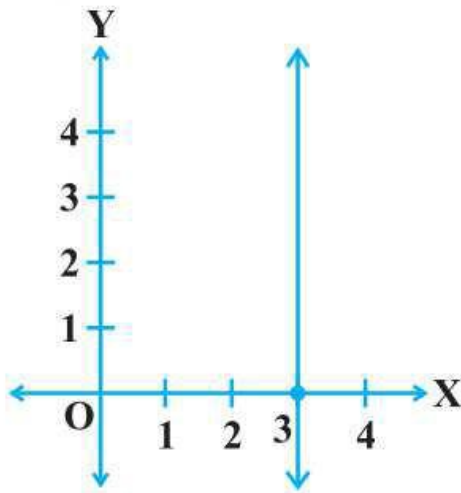
**Fig. 4.1**

**Sol.** The given equation is  $x + y = 0$ , i.e.,  $y = -x$ .

Any point on the graph of  $y = -x$ , will have  $x$  and  $y$  coordinates of opposite signs.

As the points (-1, 1) and (-3, 3) have  $x$  and  $y$  coordinates of opposite signs, so these points satisfy the given equation and the two points determine a unique line, hence the given statement is true.

4. **The graph given below represents the linear equation  $x = 3$  (see Fig. 4.2).**
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**Fig. 4.2**

**Sol.** We know that the graph of the equation  $x = a$  is a line parallel to the  $y$ -axis and to the right of  $y$ -axis, if  $a > 0$ .  
The given statement is true, since the graph is a line parallel to  $y$ -axis at a distance of 3 units to the right of it.

**5. The coordinates of points in the table:**

<b>X</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>
<b>y</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>-5</b>	<b>6</b>

**Represent some of the solution of the equation  $x - y + 2 = 0$ .**

**Sol.** The points  $(0, 2)$ ,  $(1, 3)$ ,  $(2, 4)$  and  $(4, 6)$  satisfy the given equation  $x - y + 2 = 0$ . Each of these points is the solution of the equation  $x - y + 2 = 0$ . But, they do not satisfy the given equation as  $3 - (-5) + 2 = 0$ , i.e.,  $3 + 5 + 2 = 0$  or  $10 = 0$ , which is false.  
Hence, the given statement is false, since the point  $(3, -5)$  does not satisfy the given equation.

**6. Every point on the graph of a linear equation in two variables does not represent a solution of the linear equation.**

**Sol.** As every point on the graph of linear equation in two variables represents a solution of the equation, so the given statement is false.

**7. The graph of every linear equation in two variables need not be a line.**

**Sol.** As the graph of a linear equation in two variables is always a line, so the given statement is false.

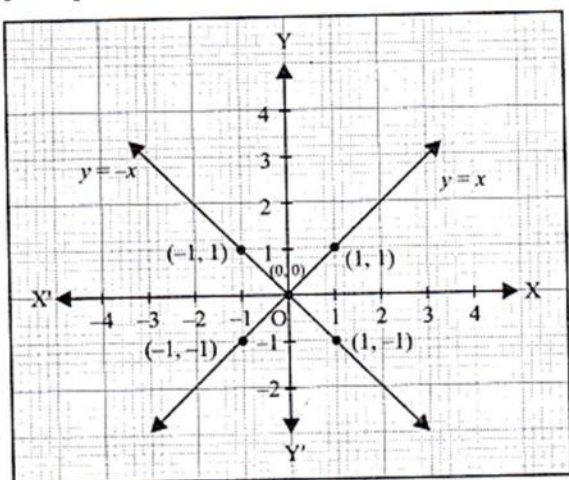
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## Linear Equations in Two Variables

### Exercise 4.3

1. Draw the graphs of linear equations  $y = x$  and  $y = -x$  on the same Cartesian plane. What do you observe?

**Sol.** Any point on the graph of  $y = x$  will have  $x$  and  $y$  coordinates same. The line passes through the points  $(0, 0)$ ,  $(1, 1)$  and  $(-1, -1)$ .  
Again, any point on the graph of  $y = -x$  will have  $x$  and  $y$  coordinates of opposite signs. The line passes through the points  $(1, -1)$  and  $(-1, 1)$ .  
Also,  $(0, 0)$  satisfy  $y = -x$ .  
The graph of linear equation  $y = x$  and  $y = -x$  on the same Cartesian plane is shown in the figure given below.



We observe that the graph of these equation passes through  $(0, 0)$ .

2. Determine the point on the graph of the linear equation  $2x + 5y = 19$ , whose ordinate is  $1\frac{1}{2}$  times its abscissa.

**Sol.** Let the coordinate of the point be  $(2, 3)$ .

Now, for  $x = 2$  and  $y = 3$ .

$$2x + 5y = 2(2) + 5(3) = 4 + 15 = 19$$

Therefore, the point  $(2, 3)$  is a solution of the equation  $2x + 5y = 19$ .

Abscissa of the point is 2 and ordinate is 3.

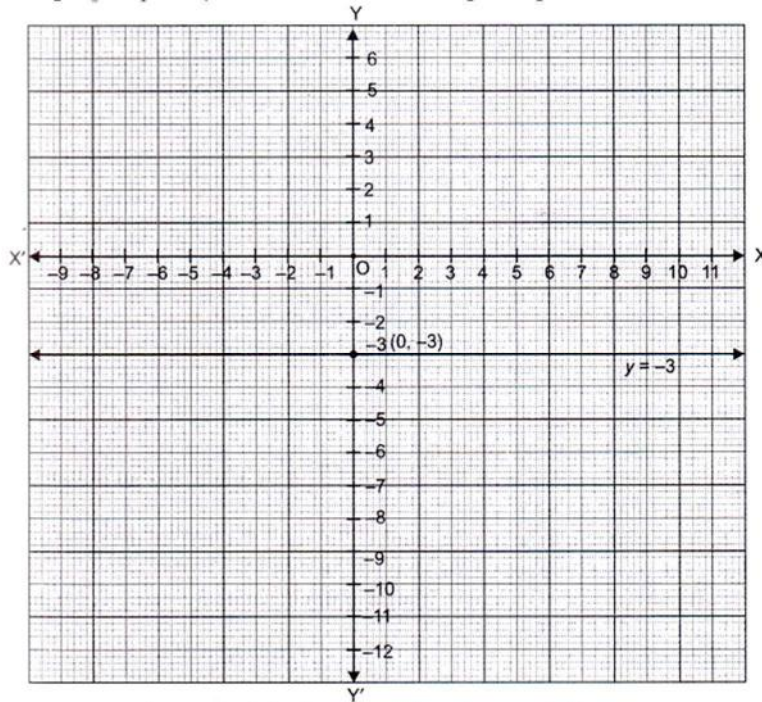
$$\text{Now, } 2 \times 1\frac{1}{2} = 2 \times \frac{3}{2} = 3$$

So, ordinate of the point  $(2, 3)$  is  $1\frac{1}{2}$  times its abscissa.

3. Draw the graph of the equation represented by a straight line which is parallel to the  $x$ -axis and at a distance 3 units below it.
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**Sol.** The graph of the equation  $y = -3$  is a line parallel to the axis and at a distance 3 units below it. So, graph of the equation  $y = -3$  is a line parallel to x-axis and passing through the point  $(0, -3)$  as shown in the figure given below:



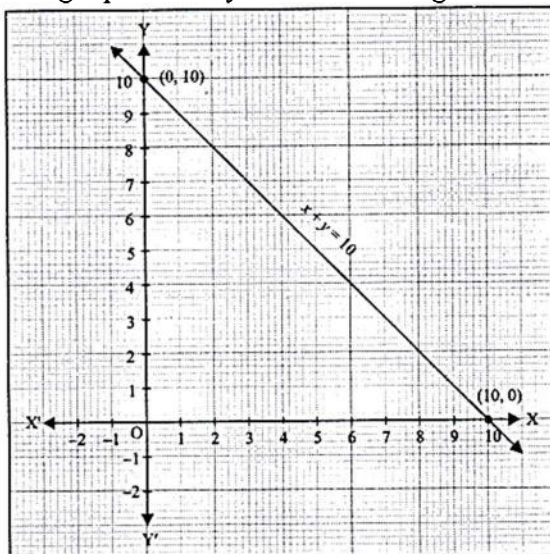
**4. Draw the graph of the linear equation whose solutions are represented by the points having the sum of coordinates as 10 units.**

**Sol.** A linear equation whose solutions are represented by the points having the sum of coordinates as 10 units is  $x + y = 10$ .

When  $x = 0$ ,  $y = 10$  and when  $x = 10$ ,  $y = 0$ .

Now, plot these two points  $(0, 10)$  and  $(10, 0)$  on a graph paper and join them to obtain a straight line.

The graph of  $x + y = 10$  is a straight line as shown in the figure given below.



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5. Write the linear equation such that each point on its graph has an ordinate 3 times its abscissa.

Sol. A linear equation such that each point on its graph has an ordinate 3 times its abscissa is  $y = 3x$ .

6. If the point (3, 4) lies on the graph of  $3y = ax + 7$ , then find the value of a.

Sol. The point (3, 4) lies on the graph of  $3y = ax + 7$ .

Substituting  $x = 3$  and  $y = 4$  in the given equation  $3y = ax + 7$ , we get

$$\therefore 3 \times 4 = a \times 3 + 7$$

$$\Rightarrow 12 = 3a + 7 \Rightarrow 3a = 5 \Rightarrow a = \frac{5}{3}$$

7. How many solution(s) of the equation  $2x + 1 = x - 3$  are there on the:

(i) Number line

(ii) Cartesian plane?

Sol. (i) The number of solution(s) of the equation  $2x + 1 = x - 3$  which are on the number line is one.

$$2x + 1 = x - 3 \Rightarrow 2x - x = -3 - 1 \Rightarrow x = -4$$

$\therefore x = -4$  is the solution of the given equation.

(ii) The number of solution(s) of the equation  $2x + 1 = x - 3$  which are on the Cartesian plane are infinitely many solutions.

8. Find the solution of the linear equation  $x + 2y = 8$  which represents a point on

(i) x-axis (ii) y-axis

Sol. We know that the point which lies on x-axis has its ordinate 0.

Putting  $y = 0$  in the equation  $x + 2y = 8$ , we get

$$x + 2(0) = 8 \Rightarrow x = 8$$

A point which lies on y-axis has its abscissa 0.

Putting  $x = 0$  in the equation  $x + 2y = 8$ , we get

$$0 + 2y = 8 \Rightarrow y = 4$$

9. For what value of c, the linear equation  $2x + cy = 8$  has equal values of x and y for its solution.

Sol. The value of c for which the linear equation  $2x + cy = 8$  has equal values of x and y

i.e.,  $x = y$  for its solution is

$$2x + cy = 8 \Rightarrow 2x + cx = 8 \quad [ \because y = x ]$$

$$\Rightarrow cx = 8 - 2x$$

$$\therefore c = \frac{8 - 2x}{x}, x \neq 0$$

10. Let y varies directly as x. If  $y = 12$  when  $x = 4$ , then write a linear equation. What is the value of y when  $x = 5$ ?

Sol. y varies directly as x.

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$$\Rightarrow y \propto x,$$

$$\therefore y = kx$$

Substituting  $y = 12$  when  $x = 4$ , we get

$$12 = k \times 4 \Rightarrow k = 12 \div 4 = 3$$

Hence, the required equation is  $y = 3x$ .

The value of  $y$  when  $x = 5$  is  $y = 3 \times 5 = 15$ .

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## Linear Equations in Two Variables

### Exercise 4.4

1. Show that the points A (1, 2), B (-1, -16) and C (0, -7) lie on the graph of the linear equation  $y = 9x - 7$ .

**Sol.** For A (1, 2), we have  $2 = 9(1) - 7 = 9 - 7 = 2$

For B (-1, -16), we have  $-16 = 9(-1) - 7 = -9 - 7 = -16$

For C (0, -7), we have  $-7 = 9(0) - 7 = 0 - 7 = -7$

We see that the line  $y = 9x - 7$  is satisfied by the points A (1, 2), B (-1, -16) and C (0, -7).

Therefore, A (1, 2), B (-1, -16) and C (0, -7) are solutions of the linear equation  $y = 9x - 7$  and therefore, lie on the graph of the linear equation  $y = 9x - 7$ .

2. The following observed values of x and y are thought to satisfy a linear equation.

x	6	-6
y	-2	6

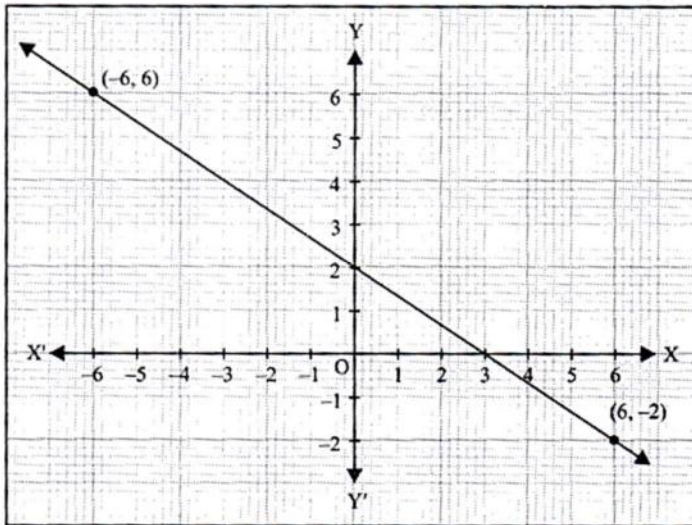
Write the linear equation.

Draw the graph using the values of x, y given in the above table. At what points the graph of the linear equation

(i) cuts the x-axis (ii) cuts the y-axis

**Sol.** The linear equation is  $2x + 3y = 6$ . Both the points (6, -2) and (-6, 6) satisfy the given linear equation.

Plot the points (-6, 2) and (-6, 6) on a graph paper. Now join these two points and obtain a line. We see that the graph cuts the x-axis at (3, 0) and y-axis at (0, 2).



3. Draw the graph of the linear equation  $3x + 4y = 6$ . At what points, the graph cuts the x-axis and the y-axis.

**Sol.** The solutions of the linear equation

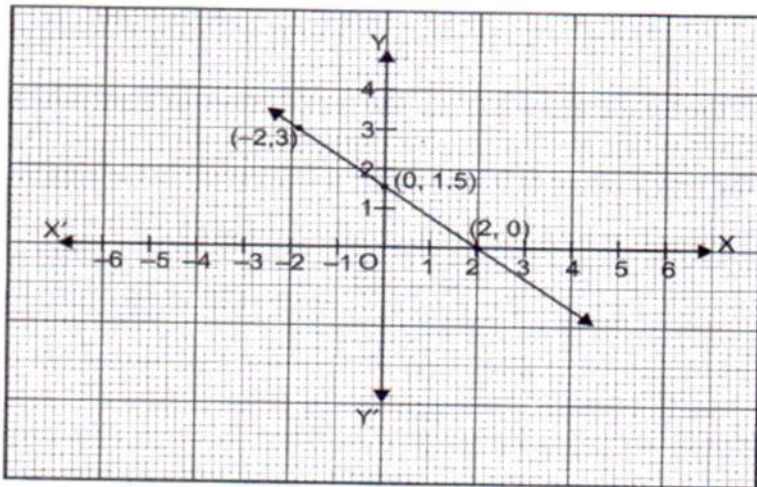
$$3x + 4y = 6$$

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Can be expressed in the form of a table as follows by writing the values of y below the corresponding value of x:

X	2	-2	0
y	0	3	1.5

Now plot the points (2, 0), (-2, 3) and (0, 1.5) on a graph paper. Now, join the points and obtain a line.



We see that the graph cuts the x-axis at (2, 0) and y-axis at (0, 1.5).

4. **The linear equation that converts Fahrenheit (F) to Celsius ( $^{\circ}\text{C}$ ) is given by the relation:**

$$C = \frac{5F - 160}{9}$$

- (i) If the temperature is  $86^{\circ}\text{F}$ , what is the temperature in Celsius?  
 (ii) If the temperature is  $35^{\circ}\text{C}$ , what is the temperature in Fahrenheit?  
 (iii) If the temperature is  $0^{\circ}\text{C}$  what is the temperature in Fahrenheit and if the temperature is  $0^{\circ}\text{F}$ , what is the temperature in Celsius?  
 (iv) What is the numerical value of the temperature which is same in both the scales?

**Sol.**  $C = \frac{5F - 160}{9}$

(i) Putting  $F = 86^{\circ}$ , we get  $C = \frac{5(86) - 160}{9} = \frac{430 - 160}{9} = \frac{270}{9} = 30^{\circ}$

Hence, the temperature in Celsius is  $30^{\circ}\text{C}$ .

(ii) Putting  $C = 35^{\circ}$ , we get  $35^{\circ} = \frac{5(F) - 160}{9} \Rightarrow 315^{\circ} = 5F - 160$

$$\Rightarrow 5F = 315 + 160 = 475$$

$$\therefore F = \frac{475}{5} = 95^{\circ}$$

Hence, the temperature in Fahrenheit is  $95^{\circ}\text{F}$ .

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(iii) Putting  $C = 0^\circ$ , we get

$$0 = \frac{5F - 160}{9} \Rightarrow 0 = 5F - 160$$

$$\Rightarrow 5F = 160$$

$$\therefore F = \frac{160}{5} = 32^\circ$$

Now, putting  $F = 0^\circ$ , we get

$$C = \frac{5F - 160}{9} \Rightarrow C = \frac{5(0) - 160}{9} = \left(-\frac{160}{9}\right)^\circ$$

If the temperature is  $0^\circ$  C, the temperature in Fahrenheit is  $32^\circ$  and if the temperature is  $0^\circ$  F, then the temperature in Celsius is  $\left(-\frac{160}{9}\right)^\circ$  C.

(iv) Putting  $C = F$ , in the given relation, we get

$$F = \frac{5F - 160}{9} \Rightarrow 9F = 5F - 160$$

$$\Rightarrow 4F = -160$$

$$\therefore F = \frac{-160}{4} = -40^\circ$$

Hence, the numerical value of the temperature which is same in both the scales is  $-40$ .  
The linear equation that converts Kelvin ( $x$ ) to Fahrenheit ( $y$ ) is given by the relation:

$$y = \frac{9}{5}(x - 273) + 32$$

5. **If the temperature of a liquid can be measured in Kelvin units as  $x^\circ$  K or in Fahrenheit units as  $y^\circ$  F, the relation between the two systems of measurement of temperature is given by the linear equation**

$$y = \frac{9}{5}(x - 273) + 32$$

**(i) Find the temperature of the liquid in Fahrenheit if the temperature of the liquid is  $313^\circ$  K.**

**(ii) If the temperature is  $158^\circ$  F, then find the temperature in Kelvin.**

**Sol.**  $y = \frac{9}{5}(x - 273) + 32$

(i) When the temperature of the liquid is  $x = 313^\circ$  K

$$y = \frac{9}{5}(313 - 273) + 32 = \frac{9}{5} \times 40 + 32 = 72^\circ + 32^\circ = 104^\circ F$$

(ii) When the temperature of the liquid is  $y = 158^\circ$  F

$$158 = \frac{9}{5}(x - 273) + 32 \Rightarrow \frac{9}{5}(x - 273) = 158 - 32$$

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$$\Rightarrow x - 273 = 126 \times \frac{5}{6} = 70$$

$$\Rightarrow x - 273 = 70 = 273 + 70 = 343^0 K$$

6. **The force exerted to pull a cart is directly proportional to the acceleration produced in the body. Express the statement as a linear equation in two variables and draw the graph of the same by taking the constant mass equal to 6 kg. Read from the graph, the force required when the acceleration produced is (i) 5 m/sec<sup>2</sup>, (ii) 6 m/sec<sup>2</sup>.**

**Sol.** We have  $y \propto x \Rightarrow y = mx$

Where y denotes the force, x denotes the acceleration and m denotes the constant mass.

Taking  $m = 6\text{kg}$ , we get  $y = 6x$

Now, we form a table as follows by writing the value of y below the corresponding value of x.

X	0	1	2
y	0	6	12

Plot the points (0, 0), (1, 6) and (2, 12) on a graph paper and join any two points and obtain a line.

