Chapter Thirteen

KINETIC THEORY



MCQ I

- A cubic vessel (with faces horizontal + vertical) contains an ideal 13.1 gas at NTP. The vessel is being carried by a rocket which is moving at a speed of 500m s^{-1} in vertical direction. The pressure of the gas inside the vessel as observed by us on the ground
 - (a) remains the same because 500m s^{-1} is very much smaller than v_{rms} of the gas.
 - (b) remains the same because motion of the vessel as a whole does not affect the relative motion of the gas molecules and the walls.
 - (c) will increase by a factor equal to $\left(v_{ms}^2 + (500)^2\right)/v_{ms}^2$ where $v_{\rm rms}$ was the original mean square velocity of the gas. (d) will be different on the top wall and bottom wall of the vessel.
- 1 mole of an ideal gas is contained in a cubical volume V, 13.2 ABCDEFGH at 300 K (Fig. 13.1). One face of the cube (EFGH) is made up of a material which totally absorbs any gas molecule

incident on it. At any given time,

- (a) the pressure on EFGH would be zero.
- (b) the pressure on all the faces will the equal.
- (c) the pressure of EFGH would be double the pressure on ABCD.
- (d) the pressure on EFGH would be half that on ABCD.

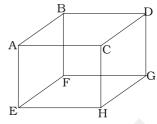


Fig. 13.1

- **13.3** Boyle's law is applicable for an
 - (a) adiabatic process.
 - (b) isothermal process.
 - (c) isobaric process.
 - (d) isochoric process.
- **13.4** A cylinder containing an ideal gas is in vertical position and has a piston of mass M that is able to move up or down without friction (Fig. 13.2). If the temperature is increased,

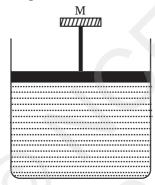


Fig. 13.2

- (a) both p and V of the gas will change.
- (b) only p will increase according to Charle's law.
- (c) V will change but not p.
- (d) p will change but not V.
- Volume versus temperature graphs for a given mass of an ideal gas are shown in Fig. 13.3 at two different values of constant pressure. What can be inferred about relation between $P_1 \& P_2$?

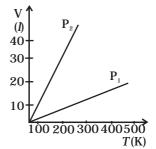


Fig.13.3

- (a) $P_1 > P_2$
- (b) $P_1 = P_2$
- (c) $P_1 < P_2$
- (d) data is insufficient.

- 13.6 1 mole of H_2 gas is contained in a box of volume $V = 1.00 \text{ m}^3$ at T = 300 K. The gas is heated to a temperature of T = 3000 K and the gas gets converted to a gas of hydrogen atoms. The final pressure would be (considering all gases to be ideal)
 - (a) same as the pressure initially.
 - (b) 2 times the pressure initially.
 - (c) 10 times the pressure initially.
 - (d) 20 times the pressure initially.
- A vessel of volume V contains a mixture of 1 mole of Hydrogen and 1 mole of Oxygen (both considered as ideal). Let $f_1(v)dv$, denote the fraction of molecules with speed between v and (v + dv) with $f_2(v)dv$, similarly for oxygen. Then
 - (a) $f_1(v) + f_2(v) = f(v)$ obeys the Maxwell's distribution law.
 - (b) $f_1(v)$, $f_2(v)$ will obey the Maxwell's distribution law separately.
 - (c) Neither f_1 (v), nor f_2 (v) will obey the Maxwell's distribution law.
 - (d) f_2 (v) and f_1 (v) will be the same.
- **13.8** An inflated rubber balloon contains one mole of an ideal gas, has a pressure p, volume V and temperature T. If the temperature rises to 1.1 T, and the volume is increaset to 1.05 V, the final pressure will be
 - (a) 1.1 p
 - (b) p
 - (c) less than p
 - (d) between p and 1.1.

MCQ II

ABCDEFGH is a hollow cube made of an insulator (Fig. 13.4). Face ABCD has positive charge on it. Inside the cube, we have ionized hydrogen.

The usual kinetic theory expression for pressure

- (a) will be valid.
- (b) will not be valid since the ions would experience forces other than due to collisions with the walls.
- (c) will not be valid since collisions with walls would not be elastic.
- (d) will not be valid because isotropy is lost.
- Fig. 13.4

В

+P

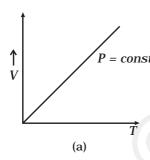
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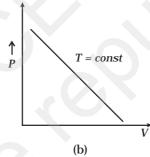
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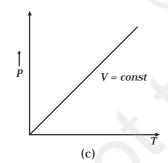
13.10 Diatomic molecules like hydrogen have energies due to both translational as well as rotational motion. From the equation in

kinetic theory $pV = \frac{2}{3}E$, E is

- (a) the total energy per unit volume.
- (b) only the translational part of energy because rotational energy is very small compared to the translational energy.
- (c) only the translational part of the energy because during collisions with the wall pressure relates to change in linear momentum.
- (d) the translational part of the energy because rotational energies of molecules can be of either sign and its average over all the molecules is zero.
- **13.11** In a diatomic molecule, the rotational energy at a given temperature
 - (a) obeys Maxwell's distribution.
 - (b) have the same value for all molecules.
 - (c) equals the translational kinetic energy for each molecule.
 - (d) is (2/3)rd the translational kinetic energy for each molecule.
- **13.12** Which of the following diagrams (Fig. 13.5) depicts ideal gas behaviour?







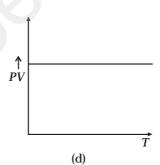


Fig. 13.5

- **13.13** When an ideal gas is compressed adiabatically, its temperature rises: the molecules on the average have more kinetic energy than before. The kinetic energy increases,
 - (a) because of collisions with moving parts of the wall only.
 - (b) because of collisions with the entire wall.

- (c) because the molecules gets accelerated in their motion inside the volume.
- (d) because of redistribution of energy amongst the molecules.

VSA

- **13.14** Calculate the number of atoms in 39.4 g gold. Molar mass of gold is 197g mole⁻¹.
- **13.15** The volume of a given mass of a gas at 27°C, 1 atm is 100 cc. What will be its volume at 327°C?
- 13.16 The molecules of a given mass of a gas have root mean square speeds of $100\,\mathrm{m\,s^{-1}}$ at $27\,^{\circ}\mathrm{C}$ and 1.00 atmospheric pressure. What will be the root mean square speeds of the molecules of the gas at $127\,^{\circ}\mathrm{C}$ and 2.0 atmospheric pressure?
- 13.17 Two molecules of a gas have speeds of $9 \times 10^6 \, m \, s^{-1}$ and $1 \times 10^6 \, m \, s^{-1}$, respectively. What is the root mean square speed of these molecules.
- **13.18** A gas mixture consists of 2.0 moles of oxygen and 4.0 moles of neon at temperature *T*. Neglecting all vibrational modes, calculate the total internal energy of the system. (Oxygen has two rotational modes.)
- 13.19 Calculate the ratio of the mean free paths of the molecules of two gases having molecular diameters 1 Å and 2 Å. The gases may be considered under identical conditions of temperature, pressure and volume.

SA

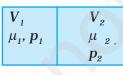


Fig 13.6

- 13.20 The container shown in Fig. 13.6 has two chambers, separated by a partition, of volumes $V_1 = 2.0$ litre and $V_2 = 3.0$ litre. The chambers contain $\mu_1 = 4.0$ and $\mu_2 = 5.0$ moles of a gas at pressures $p_1 = 1.00$ atm and $p_2 = 2.00$ atm. Calculate the pressure after the partition is removed and the mixture attains equilibrium.
- **13.21** A gas mixture consists of molecules of types A, B and C with masses $m_A > m_B > m_C$. Rank the three types of molecules in decreasing order of (a) average K.E., (b) rms speeds.

- 13.22 We have 0.5 g of hydrogen gas in a cubic chamber of size 3cm kept at NTP. The gas in the chamber is compressed keeping the temperature constant till a final pressure of 100 atm. Is one justified in assuming the ideal gas law, in the final state?
 - (Hydrogen molecules can be consider as spheres of radius 1 $\overset{o}{\rm A}$).
- **13.23** When air is pumped into a cycle tyre the volume and pressure of the air in the tyre both are increased. What about Boyle's law in this case?
- **13.24** A ballon has 5.0 g mole of helium at 7°C. Calculate
 - (a) the number of atoms of helium in the balloon,
 - (b) the total internal energy of the system.
- **13.25** Calculate the number of degrees of freedom of molecules of hydrogen in 1 cc of hydrogen gas at NTP.
- 13.26 An insulated container containing monoatomic gas of molar mass m is moving with a velocity \mathbf{v}_o . If the container is suddenly stopped, find the change in temperature.

LA

- **13.27** Explain why
 - (a) there is no atmosphere on moon.
 - (b) there is fall in temperature with altitude.
- **13.28** Consider an ideal gas with following distribution of speeds.

Speed (m/s)	% of molecules
200	10
400	20
600	40
800	20
1000	10

- (i) Calculate V_{rms} and hence T. ($m = 3.0 \times 10^{-26} \text{kg}$)
- (ii) If all the molecules with speed 1000 m/s escape from the system, calculate new V_{rms} and hence T.

- 13.29 Ten small planes are flying at a speed of 150 km/h in total darkness in an air space that is $20 \times 20 \times 1.5 \text{ km}^3$ in volume. You are in one of the planes, flying at random within this space with no way of knowing where the other planes are. On the average about how long a time will elapse between near collision with your plane. Assume for this rough computation that a saftey region around the plane can be approximated by a sphere of radius 10m.
- **13.30** A box of 1.00m^3 is filled with nitrogen at 1.50 atm at 300K. The box has a hole of an area 0.010 mm². How much time is required for the pressure to reduce by 0.10 atm, if the pressure outside is 1 atm.
- 13.31 Consider a rectangular block of wood moving with a velocity v_0 in a gas at temperature T and mass density ρ . Assume the velocity is along x-axis and the area of cross-section of the block perpendicular to v_0 is A. Show that the drag force on the block is $4\rho A v_0 \sqrt{\frac{kT}{m}}$, where m is the mass of the gas molecule.